Python course materials

# Custom Widget

## Exploring the Lorenz System of Differential Equations

In this Notebook we explore the Lorenz system of differential equations:

This is one of the classic systems in non-linear differential equations. It exhibits a range of different behaviors as the parameters (, , ) are varied.

## Imports

First, we import the needed things from IPython, [NumPy](http://www.numpy.org/), [Matplotlib](http://matplotlib.org/index.html) and [SciPy](http://www.scipy.org/). Check out the class [Python for Data Science and Machine Learning Bootcamp](https://www.udemy.com/python-for-data-science-and-machine-learning-bootcamp/) if you’re interested in learning more about this part of Python!

%matplotlib inline

from ipywidgets import interact, interactive  
from IPython.display import clear\_output, display, HTML

import numpy as np  
from scipy import integrate  
  
from matplotlib import pyplot as plt  
from mpl\_toolkits.mplot3d import Axes3D  
from matplotlib.colors import cnames  
from matplotlib import animation

## Computing the trajectories and plotting the result

We define a function that can integrate the differential equations numerically and then plot the solutions. This function has arguments that control the parameters of the differential equation (, , ), the numerical integration (N, max\_time) and the visualization (angle).

def solve\_lorenz(N=10, angle=0.0, max\_time=4.0, sigma=10.0, beta=8./3, rho=28.0):  
  
 fig = plt.figure();  
 ax = fig.add\_axes([0, 0, 1, 1], projection='3d');  
 ax.axis('off')  
  
 # prepare the axes limits  
 ax.set\_xlim((-25, 25))  
 ax.set\_ylim((-35, 35))  
 ax.set\_zlim((5, 55))  
   
 def lorenz\_deriv(x\_y\_z, t0, sigma=sigma, beta=beta, rho=rho):  
 """Compute the time-derivative of a Lorenz system."""  
 x, y, z = x\_y\_z  
 return [sigma \* (y - x), x \* (rho - z) - y, x \* y - beta \* z]  
  
 # Choose random starting points, uniformly distributed from -15 to 15  
 np.random.seed(1)  
 x0 = -15 + 30 \* np.random.random((N, 3))  
  
 # Solve for the trajectories  
 t = np.linspace(0, max\_time, int(250\*max\_time))  
 x\_t = np.asarray([integrate.odeint(lorenz\_deriv, x0i, t)  
 for x0i in x0])  
   
 # choose a different color for each trajectory  
 colors = plt.cm.jet(np.linspace(0, 1, N));  
  
 for i in range(N):  
 x, y, z = x\_t[i,:,:].T  
 lines = ax.plot(x, y, z, '-', c=colors[i])  
 \_ = plt.setp(lines, linewidth=2);  
  
 ax.view\_init(30, angle)  
 \_ = plt.show();  
  
 return t, x\_t

Let’s call the function once to view the solutions. For this set of parameters, we see the trajectories swirling around two points, called attractors.

t, x\_t = solve\_lorenz(angle=0, N=10)

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Using IPython’s interactive function, we can explore how the trajectories behave as we change the various parameters.

w = interactive(solve\_lorenz, angle=(0.,360.), N=(0,50), sigma=(0.0,50.0), rho=(0.0,50.0))  
display(w);

Failed to display Jupyter Widget of type interactive.

If you’re reading this message in the Jupyter Notebook or JupyterLab Notebook, it may mean that the widgets JavaScript is still loading. If this message persists, it likely means that the widgets JavaScript library is either not installed or not enabled. See the Jupyter Widgets Documentation for setup instructions.

If you’re reading this message in another frontend (for example, a static rendering on GitHub or NBViewer), it may mean that your frontend doesn’t currently support widgets.

The object returned by interactive is a Widget object and it has attributes that contain the current result and arguments:

t, x\_t = w.result

w.kwargs

{'N': 10,  
 'angle': 0.0,  
 'beta': 2.6666666666666665,  
 'max\_time': 4.0,  
 'rho': 28.0,  
 'sigma': 10.0}

After interacting with the system, we can take the result and perform further computations. In this case, we compute the average positions in , and .

xyz\_avg = x\_t.mean(axis=1)

xyz\_avg.shape

(10, 3)

Creating histograms of the average positions (across different trajectories) show that on average the trajectories swirl about the attractors.

*NOTE: These will look different from the lecture version if you adjusted any of the sliders in the* interactive *widget and changed the parameters.*

plt.hist(xyz\_avg[:,0])  
plt.title('Average $x(t)$');

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plt.hist(xyz\_avg[:,1])  
plt.title('Average $y(t)$');

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# Conclusion

Hopefully you’ve enjoyed using widgets in the Jupyter Notebook system and have begun to explore the other GUI possibilities for Python!